

## Chapter 2 Risk Management

1)  $\text{VaR}_{t \text{ days}} = Z \text{ Score} \times \text{SD}_{t \text{ days}}$

2)  $\text{SD}_{t \text{ days}} = \text{SD}_{1 \text{ day}} \times \sqrt{t \text{ days}}$

$$\text{VaR}_{t \text{ days}} = Z \text{ Score} \times \text{SD}_{1 \text{ day}} \times \sqrt{t \text{ days}}$$

i.e.

$$\text{VaR}_{t \text{ days}} = Z \text{ Score} \times \text{SD}_{t \text{ days}}$$

$$\text{VaR}_{t \text{ days}} = \text{VaR}_{1 \text{ day}} \times \sqrt{t \text{ days}}$$

## Chapter 3 Security Analysis

### 1) Dividend Growth Model

$$P(0) = \frac{D(1)}{(k-g)}$$

With growth,

$$P(0) = \frac{D_0(1+g)}{(k-g)}$$

### 2) PE Multiple Approach

$$P(0) = \frac{bE(1)}{(k-g)}$$

or

$$P(0) = \frac{bE_0(1+g)}{(k-g)}$$

$$3) \quad \mathbf{ABI} = \frac{(\text{No. of Advancing Stocks} - \text{No. of Declining Stocks})}{\text{Total Issues Traded}}$$

Total Issues Traded = Advancing Stocks + Declining Stocks + Stocks

$$4) \quad \mathbf{Confidence Index} = \frac{\text{Avg YTM (Best Grade Bonds)}}{\text{Avg YTM (Intermediate Grade Bonds)}}$$

$$5) \quad \mathbf{RSI} = (\% \text{ Change in Stock price}) / (\% \text{ Change in Index})$$

### 6) Arithmetic (Simple) Moving Average (AMA):

$$\mathbf{AMA}_{n,t} = \frac{1}{n} [P_t + P_{t-1} + \dots + P_{t-(n-1)}]$$

i. e.

$$\mathbf{AMA}_{n,t} = \frac{\text{Total of the closing prices in a data}}{\text{number of observation}}$$

### 7) Exponential (Weighted) Moving Average (EMA):

$$\mathbf{EMA} = [\text{CP} \times e] + [\text{Previous EMA} \times (1-e)]$$

CP = Current Closing Price,  $e = \text{exponent in decimals} = 2/n+1$

**8) Run Test Analysis:**

1. Total Number of Runs (r)
2. Number of positive price changes (n<sub>1</sub>)
3. Number of negative price changes (n<sub>2</sub>)
4. Mean ( $\mu$ ) =  $\frac{2n_1 n_2}{n_1 + n_2} + 1$
5. Standard Deviation ( $\sigma$ ) =  $\sqrt{\frac{2n_1 n_2 (2n_1 n_2 - n_2 - n_1)}{(n_1 + n_2)^2 (n_1 + n_2 - 1)}}$
6. Lower limit: [ $\mu - t (\sigma)$ ]
7. Upper limit: [ $\mu + t (\sigma)$ ]

Where, t = value from t table at the confidence level (5%) for given degrees of freedom (between 5.76596)

**9) Explain Buy and Sell Signals Provided by Moving Average Analysis**

| Buy Signal   | Sell Signal  |
|--|--|
| Stock price line rise through the moving average line when graph of the moving average line is flattering out.             | Stock price line falls through moving average line when graph of the moving average line is flattering out.                |
| Stock price line falls below moving average line which is rising.  | Stock price line rises above moving average line which is falling.   |
| Stock price line which is above moving average line falls but begins to rise again before reaching the moving average line | Stock price line which is slow moving average line rises but begins to fall again before reaching the moving average line. |

## Chapter 4 Security Valuation

### 1) Internal Rate of Return Factor:

$$\text{Internal rate of Return Factor} = \frac{\text{Net initial investment}}{\text{Annual cash inflow}}$$

### 2) CAPM:

$$R_x = R_f + \beta_x (R_m - R_f)$$

### 3) Valuation

#### 1. Dividend Based:

##### i. Single Period Holding

$$\frac{D_1}{(1 + K_e)^1} + \frac{P_1}{(1 + K_e)^1}$$

##### ii. Multi Period Holding

###### a. Zero Growth Model:

$$P = \frac{D}{K_e}$$

###### b. Constant Growth Model:

$$P = \left[ \frac{D_0(1+g)}{K_e - g} \right]$$

###### c. Variable Growth Model:

###### • Two Stage Dividend Discount Model

$$P_0 = \left[ \frac{D_0(1+g_1)}{(1+K_e)^1} + \frac{D_1(1+g_1)}{(1+K_e)^2} + \dots + \frac{D_{n-1}(1+g_1)}{(1+K_e)^n} \right] + \frac{P_n}{(1+K_e)^n}$$

###### • Three Stage Dividend Discount Model

$$P_0 = \left[ \frac{D_0(1+g_n)}{(K_e - g_n)} + \frac{D_0 H_1 (g_n + g_c)}{k_e + g_n} \right]$$

###### • H Model

## 4. Security Valuation

$$\left[ \frac{D_0(1+g_1)}{(1+K_e)^1} + \frac{D_1(1+g_1)}{(1+K_e)^2} + \frac{D_2(1+g_1)}{(1+K_e)^3} \right] + \left[ \frac{D_3(1+g_2)}{(1+K_e)^4} + \frac{D_4(1+g_2)}{(1+K_e)^5} + \dots + \frac{D_{n-1}(1+g_2)}{(1+K_e)^n} \right] + \frac{P_n}{(1+K_e)^n}$$

### 2. Earning Based

#### i. Gordons Model

$$\frac{EPS_1(1-b)}{K_e - br}$$

#### ii. Walters Model

$$P = \frac{D + \frac{r}{K_e}(E-D)}{K_e}$$

#### iii. PE Multiplier

Market Price = EPS x PE Ratio

$$EPS = \frac{\text{PAT-Preference Dividend}}{\text{No. of Equity Shares}}$$

### 3. Enterprise Value

EV = Market Value of Equity

+ Market Value of Preferred Equity

+ Market Value of Debt

+ Minority Interest

- Cash and Investments.

#### i. Enterprise value to EBITDA Multiple

$$\text{Enterprise Multiple} = \frac{\text{Enterprise Value}}{\text{EBITDA}}$$

#### ii. Enterprise value to Sales multiple

$$\text{Enterprise Multiple} = \frac{\text{Enterprise Value}}{\text{Sales}}$$

### 4) Free Cash Flows to Firm (FCFF):

#### 1. Based on its Net Income:

$$\text{FCFF} = \text{EAT} + I(1-t) + D \text{ -/+ Capex -/+ } \Delta\text{WC}$$

**2. Based on Operating Income or Earnings Before Interest and Tax (EBIT):**

$$\text{FCFF} = \text{EBIT} (1-t) + D \text{ -/+ Capex -/+ } \Delta \text{ Non Cash WC}$$

**3. Based on Earnings before Interest, Tax, Depreciation and Amortization (EBITDA):**

$$\text{FCFF} = \text{EBITDA} (1-t) + D * \text{ tax rate -/+ Capex -/+ } \Delta \text{Non Cash WC}$$

**4. Based on Free Cash Flow to Equity (FCFE):**

$$\text{FCFF} = \text{FCFE} + I (1-t) + \text{Principal Prepaid} - \text{New Debt} + \text{Pref. Dividend}$$

**5. Free Cash Flows to Equity (FCFE)**

$$\text{FCFE} = \text{EAT} + D \text{ -/+ Capex -/+ } \Delta\text{WC} + \text{New Debt} - \text{Debt Repayment}$$

**Capital Expenditure**

$$\text{Capex} = \text{Closing FA} + \text{Fixed Asset Sold} + \text{Depreciation} - \text{Opening FA}$$

**5) One Stage, Two Stage and Three Stage Model for the Valuation of the firm**

**1. For one stage Model:**

$$\text{Intrinsic Value} = \text{Present Value of Stable Period Free Cash Flows to Firm}$$

**2. For two stage Model:**

$$\text{Intrinsic Value} = \text{Present value of Explicit Period Free Cash Flows to Firm} \\ + \text{Present Value of Stable Period Free Cash Flows to a Firm,}$$

or

$$\text{Intrinsic Value} = \text{Present Value of Transition Period Free Cash Flows to Firm} \\ + \text{Present Value of Stable Period Free Cash Flows to a Firm}$$

**3. For three stage Model:**

$$\text{Intrinsic Value} = \text{Present value of Explicit Period Free Cash Flows to Firm} \\ + \text{Present Value of Transition Period Free Cash Flows to Firm} \\ + \text{Present Value of Stable Period Free Cash Flows to Firm}$$

**6) Right Share****Ex-Right Price of shares**

$$\text{Ex-Right Price } (P_1) = \frac{nP_0 + n_1S}{n + n_1}$$

**Value of the Right**

$$\text{Value of right} = \frac{\text{No. of right shares}}{\text{Total Holding (Old+New)}} \times (\text{Market price} - \text{Subscription price})$$

$$\text{Value of right} = \frac{n_1(P_0 - S)}{n + n_1}$$

Alternatively

$$\text{Value of right} = P_0 - P_1$$

Ex Right Price ( $P_1$ ) = Market Price before right issue ( $P_0$ ) – Value of the Right

**7) Value Preference Shares****1. Value of the redeemable preference shares**

$$\frac{\text{Dividend}_1}{(1+r)^1} + \frac{\text{Dividend}_2}{(1+r)^2} + \dots + \frac{(\text{Dividend}_n + \text{Maturity Value})}{(1+r)^n}$$

**2. Value of the irredeemable preference shares**

$$\text{MP} = \frac{\text{Preference Dividend}}{\text{Required return on Preference Shares}}$$

**8) Value of bond**

$$\text{BV} = I \times \text{PVAF}_{\text{YTM}, n} + \text{RV} \times \text{PVF}_{\text{YTM}, n}$$

Where,

BV = Value of the bond or Theoretical Market Price or Intrinsic Value of the bond [Present value of all the future cash flows]

I = Annual interest payable on the bond

RV = Redemption value of the bond. [May be at par, premium or discount]

n = maturity period of bond

YTM = yield to maturity or required rate of return or going rate on new bond with same risk

**Bond's Value with semi-annual interest rate**

$$BV = \frac{I}{2} \times PVAF_{\frac{YTM}{2}, 2n} + RV \times PVF_{\frac{YTM}{2}, 2n}$$

### 9) Current Yield

$$\text{Current Yield} = \frac{\text{Interest}}{\text{Market price}} \times 100$$

### 10) Yield to Maturity

#### 1. Average Method

$$YTM = \frac{C + \frac{(RV - MV)}{n}}{\frac{(RV + MV)}{2}}$$

#### 2. Discounted Cash Flow Method (IRR Method)

$$BV = I \times PVAF_{YTM, n} + RV \times PVF_{YTM, n}$$

Where,

BV = Theoretical Value of Bond

I = Annual Interest/Coupon Amount

PVAF = Present Value Annuity Factor

YTM = Yield to Maturity (Investors Required Rate of Investors)

PVF = Present Value Factor

### 11) Duration of Bond

#### 1. Macaulay's Duration of bond

$$\text{Mac D} = \sum \text{Weight} \times \text{Year}$$

Where,

Weight = Weight of a Present Value of cash flows in Total Present Value

#### Alternative 1

$$\text{Mac D} = \frac{\sum PV \times Yr}{\sum PV}$$

Draft Format

| Year | Cash flows | PVF @ YTM | Present Value(PV) | PV x Year |
|------|------------|-----------|-------------------|-----------|
| 1    | Interest   |           |                   |           |

## 4. Security Valuation

|   |                         |  |           |                     |
|---|-------------------------|--|-----------|---------------------|
| 2 | Interest                |  |           |                     |
| 3 | Interest                |  |           |                     |
| 4 | Interest +<br>Principal |  |           |                     |
|   |                         |  | $\sum PV$ | $\sum PV \times Yr$ |

### Alternative 2

$$\text{Mac D} = \frac{1+YTM}{YTM} - \frac{(1+YTM)^t (c-YTM)}{c [(1+YTM)^t - 1] + YTM}$$

Where,

c= coupon rate, t= Time to maturity, **YTM** = yield to maturity

### Alternative 3

$$\text{MacD} = \frac{\sum \frac{t \cdot c}{(1+i)^t} + \frac{n \cdot M}{(1+i)^n}}{P}$$

Where,

n= no. of cash flows,

c= coupon rate

t= Time to maturity,

i= Required yield,

M= Maturity Value,

P= Bond Price

## 2. Modified Duration (%) or Volatility of the Bond

$$\text{Volatility or Mod D} = \frac{\text{Macaulay's Duration}}{\left(1 + \frac{YTM}{n}\right)}$$

Where, n = no. of compounding in a year

### 12) Convexity

$$\text{Convexity} = \frac{PV_+ + PV_- - 2PV_0}{2PV_0 \times (\Delta \text{Yield})^2}$$

$$\% \Delta PV \approx (-\text{AnnModDur} \times \Delta \text{Yield}) + [\text{Convexity} \times (\Delta \text{Yield})^2]$$

Where,

$PV_+$  = Bonds price when yield increases

$PV_-$  = Bonds price when yield decreases

$PV_0$  = Initial Bond Price at given yield

$\Delta Y_{eild}$  = Change in Yield

AnnModDur = Annual Modified Duration

### 13) Convertible Bonds

#### 1. Conversion Ratio:

The number of shares each convertible bond converts into. It may be expressed per bond.

#### 2. Conversion Value:

Conversion Value = Market price per common share x Conversion ratio

#### 3. Conversion Premium:

The amount by which the price of a convertible security exceeds the current market value of the common stock into which it may be converted.

CP = Market price of Convertible Bond – Conversion Value

CP = MP – CV

#### 4. Conversion Premium Ratio:

Ratio which shows at what premium the convertible bond is trading in the market.

Conversion Premium Ratio =  $\frac{MV}{CV} - 1$

#### 5. Straight Value of the Bond:

It is the price where the bond would trade if it were not convertible to stock. Its then is equivalent to non-convertible bond.

#### 6. Minimum Value of the Convertible Bond:

A convertible bond should at the lowest trade at the higher of either the conversion value or straight value.

#### 7. Downside Risk:

Downside risk is the % premium over the straight value of the bond.

DR (%) =  $\left( \frac{MP}{SV} - 1 \right) \times 100$

**8. Conversion Parity Price or Market Conversion Price:**

Price at which the investor will neither gain nor lose on buying the bond and exercising it.

$$CPP = \frac{MP}{N} \times 100$$

**9. Favourable Income Differential Per Share**

It represents extra income earned in Bond over dividend income in shares.

$$FID = \frac{\text{Interest from Bond} - (\text{Dividend from Equity} \times CR)}{\text{Conversion Ratio}}$$

**10. Premium Payback Period:**

It represents the time in which we recover premium paid (to purchase the Convertible Bond) using extra income of interest.

$$PPP = \frac{\text{Conversion Premium}}{\text{Favourable Income Differential}}$$

### 1) Return of Investment in Single Security or Single Asset

$$R = \frac{\text{Forecasted Dividend} + \text{Forecasted Capital Appreciation}}{\text{Initial Investment}}$$

$$R = \frac{D + CA}{I}$$

### 2) Expected Return:

$$\bar{R} = \sum_{i=1}^n R_i P_i$$

### 3) Portfolio Return

$$R_p = \sum_{i=1}^n \bar{R}_i W_i$$

$$R_p = W_1 R_1 + W_2 R_2 + \dots + W_n R_n$$

### 4) Return of security under CAPM

$$R_i = R_f + \beta_i (R_m - R_f)$$

$$R_p = R_f + \beta_p (R_m - R_f)$$

### 5) The Arbitrage Pricing Theory Model

Stocks/Portfolios Returns according to APT will be

$$R_j = R_f + \beta_1 \lambda_1 + \beta_2 \lambda_2 + \beta_3 \lambda_3 + \dots + e_j$$

Where,

$\lambda_1, \lambda_2, \lambda_3$  are average risk premium for each of the factors in the model

$\beta_1, \beta_2, \beta_3$  are betas of the security for each of the factors

### 6) Single index model

The single index model equation is:

$$R_i = \alpha_i + \beta_i R_m + \epsilon_i$$

Where,

$R_i$  = expected return on security i

$\alpha_i$  = alpha coefficient or intercept of the straight line

$\beta_i$  = beta coefficient or slope of the line

$R_m$ =the rate of return on market index

$\epsilon_i$ =unsystematic risk of the security

### 7) Total Risk = Systematic Risk + Unsystematic Risk

### 8) Beta

#### 1. Regression Analysis

$$\beta_i = \frac{\sum XY - n\bar{X}\bar{Y}}{\sum Y^2 - n\bar{Y}^2}$$

Where,

$\beta_i$ =Beta of the stock i

X=Return(%)from the stock,

Y=Return(%) from the market

$\bar{X}$ =Expected or Mean value of returns from stock

$\bar{Y}$ =Expected or Mean value of returns from market

n=number of observation

#### 2. Correlation Analysis

$$\beta_i = \frac{\text{Corr}_{xy}\sigma_x\sigma_y}{\sigma_y^2} \text{ or } \frac{\text{Corr}_{xy}\sigma_x}{\sigma_y} \text{ or } \frac{\text{Cov}_{xy}}{\sigma_y^2}$$

Where,

$\beta_i$ =beta of the stock i

$\text{Corr}_{xy}$ =Correlation between returns of the stock and returns of the market

$\sigma_x$ =standard deviation of returns of the stock i

$\sigma_y$ =standard deviation of returns of the market index

$\sigma_y^2$ =variance of the market index

$\text{Cov}_{xy}$ =Covariance of stock x and y

#### 3. Portfolio Beta Using Weighted Average Method

$$\beta_p = \sum W_i\beta_i$$

Where,

$\beta_p$ =Portfolio Beta

$\beta_i$ =Beta of the each asset in the portfolio

$W_i$ =weight of each asset in the portfolio

## 5. Portfolio Management

| Value of Beta   | Interpretation  | Example   |
|-----------------|---|---|
| $\beta < 0$     | Asset generally moves in the opposite direction as compared to the index  | Gold, which often moves opposite to the movements of the stock market   |
| $\beta = 0$     | Movement of the asset is uncorrelated with the movement of the benchmark  | Fixed-yield asset, whose growth is unrelated to the movement of the stock market  |
| $0 < \beta < 1$ | Movement of the asset is generally in the same direction as, but less than the movement of the benchmark                | Stable, "staple" stock such as a company that makes soap. Moves in the same direction as the market at large, but less susceptible to day-to-day fluctuation. |
| $\beta = 1$     | Movement of the asset is generally in the same direction as, and about the same amount as the movement of the benchmark | A representative stock or a stock that is a strong contributor to the index itself.   |
| $\beta > 1$     | Movement of the asset is generally in the same direction as, but more than the movement of the benchmark                | Volatile stock, such as a tech stock, or stocks which are very strongly influenced by day-to-day market news.   |

### 9) Covariance:

$$\text{Cov}_{ab} = \frac{\sum [R_a - \bar{R}_a][R_b - \bar{R}_b]}{N}$$

$$\text{Cov}_{im} = \sigma_i \sigma_m r_{im}$$

### 10) Coefficient of correlation

$$r_{ab} = \frac{\text{Cov}_{ab}}{\sigma_a \sigma_b}$$

Where,

$\text{COV}_{ab}$  = Covariance between a and b

$R_a$  = Return on stock a

$R_b$  = Return on stock b

$\bar{R}_a$  = Expected or mean return on stock a

$\bar{R}_b$  = Expected or mean return on stock b

$\beta_x$  = Beta of the stock x

## 5. Portfolio Management

$\text{Corr}_{xy}$  = correlation between returns of the stock and returns of the market

$\sigma_x$  = Standard Deviation of returns of the stock i

$\sigma_y$  = Standard Deviation of returns of the market index

$\sigma_y^2$  = Variance of the market index

$\text{Cov}_{xy}$  = Covariance of stock x and y

### 11) Risk of Single Security

#### 1. Without probability

$$\sigma = \sqrt{\frac{\sum (R - \bar{R})^2}{N}}$$

N = Number of observations

#### 2. With probability

$$\sigma = \sqrt{\sum_{i=1}^n [(R - \bar{R})^2 p]}$$

p = probability of ith return

### 12) Risk of Portfolio having 2 securities/assets

$$\sigma_p^2 = w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + 2w_a w_b (r_{ab} \sigma_a \sigma_b)$$

Where,

$\sigma_p^2$  = portfolio variance,

$w_a$  = proportion of funds invested in first security,

$w_b$  = proportion of funds invested in second security,

$\sigma_a$  = Standard deviation of first security

$\sigma_b$  = Standard deviation of second security

$r_{ab}$  = correlation coefficient between the returns of the two securities

### 13) Risk of Portfolio having 3 securities/assets

$$\sigma_p^2 = w_a^2 \sigma_a^2 + w_b^2 \sigma_b^2 + w_c^2 \sigma_c^2 + 2w_a w_b (r_{ab} \sigma_a \sigma_b) + 2w_b w_c (r_{bc} \sigma_b \sigma_c) + 2w_c w_a (r_{ca} \sigma_c \sigma_a)$$

$$\sigma_p^2 = \sum_{i=1}^n \sum_{j=1}^n w_i w_j \sigma_i \sigma_j r_{ij}$$

$$\sigma_p^2 = \sum_{i=1}^n \sum_{j=1}^n w_i w_j \text{Cov}_{ij}$$

Where,

$\sigma_p^2$  = portfolio variance,

$w_i$  = proportion of funds invested in first security,

$w_m$  = proportion of funds invested in second security,

$\text{Cov}_{im}$  = covariance between the pair of securities a and b

$n$  = Total number of securities in the portfolio

#### 14) Single Index Model

##### Security Variance ( $\sigma_i^2$ )

$$\sigma^2 = \beta_i^2 \sigma_m^2 + \epsilon_i^2$$

Where,

$\sigma^2$  = total variance

$\beta_i^2 \sigma_m^2$  = systematic variance

$\sigma_{\epsilon_i}^2$  = unsystematic variance

##### Portfolio variance ( $\sigma_p^2$ )

$$\sigma_p^2 = \left[ \left( \sum W_i \beta_i \right)^2 \sigma_m^2 \right] + \left[ \sum (W_i \epsilon_i)^2 \right]$$

##### Portfolios Alpha and Beta

$$\alpha_p = \sum_{i=1}^N w_i \alpha_i$$

$$\beta_p = \sum_{i=1}^N w_i \beta_i$$

#### 15) Three market Lines:

##### 1. Capital Market Line

$$R_i = R_f + \frac{\sigma_i}{\sigma_m} (R_m - R_f)$$

$\sigma_i$  = Standard deviation of the security

$\sigma_m$  = Standard deviation of the market

##### 2. Security market line

$$R_i = R_f + \beta_i (R_m - R_f)$$

SML is the graphical representation of Capital Asset Pricing Model

##### 3. Security Characteristic Line

$$r_i = \alpha_i + \beta_i R_m$$

Where,

$r_i$ =expected return on security i

$r_f$ =alpha

$\beta_i R_m$ =component of return due to market movement

### 16) Optimum Portfolio Theory

1. Find out the “excess return to beta” ratio for each stock under consideration using Treynor ratio.
2. Rank them from the highest to the lowest.
3. Proceed to calculate  $C_i$  for all the stocks/portfolios according to the ranked order using the following formula:

$$C_i = \frac{\sigma_m^2 \sum_{i=1}^N \frac{(R_i - R_f) \beta_i}{\sigma_{ei}^2}}{1 + \sigma_m^2 \sum_{i=1}^N \frac{\beta_i^2}{\sigma_{ei}^2}}$$

Where,

$\sigma_m^2$ =Variance of the market index

$\sigma_{ei}^2$ =Variance of the stock's movement that is not associated with the movement of market index i.e stock's unsystematic risk.

4. Determine the relative  $Z_i$  investment of each stock in the selected portfolio

$$Z_i = \frac{\beta_i}{\sigma_{ei}^2} \left( \frac{R_i - R_f}{\beta_i} - C^* \right)$$

5. Find out the weight of  $X_i$  each stock in the selected portfolio

$$X_i = \frac{Z_i}{\sum_{j=1}^N Z_j}$$

### 17) Portfolio Evaluation Measures

1. Sharpe ratio =  $\frac{R_i - R_f}{\sigma_i}$

2. Treynor ratio =  $\frac{R_i - R_f}{\beta_i}$

3. Jensen's Alpha = Actual Return - Required return [CAPM return]

$$\text{Jensen's Alpha} = R_i - (R_f + \beta(R_m - R_f))$$

### 18) Minimum Variance Portfolio

$$W_A = \frac{\sigma_B^2 - \text{Cov}_{A,B}}{\sigma_A^2 + \sigma_B^2 - 2\text{Cov}_{A,B}}$$

$$W_B = 1 - W_A$$

Where,

$W_A$  = Weight of security A in minimum variance portfolio

$W_B$  = Weight of security B in minimum variance portfolio

### 19) Constant Proportion Portfolio Insurance Policy

$$\text{Equity Value} = \text{Multiplier} \times [\text{Portfolio Value} - \text{Floor Value}]$$

### 20) The covariance of returns between securities i and j

$$\text{Cov}_{ij} = \beta_i \beta_j \sigma_m^2$$

### 21) Fixed Income Portfolio

– Arithmetic Average Rate of Return

$$\text{AARR} = \frac{\sum R_i}{N}$$

$R_i$  = Returns of respective period

$N$  = no. of periods

– Time Weighted Rate of Return

$$\text{TWRR} = [(1 + R_1)(1 + R_2) \dots (1 + R_n)] - 1$$

– MWRR (IRR),  $0 = \text{PV of CIF} - \text{PV of COF}$

– Annualised Return

$$\text{ARR} = (1 + R) \times \frac{365}{\text{No. of days}}$$

$R$  = Entire return for holding period

## Chapter 7 Mutual Funds

### 1) Net Assets Value

$$\text{NAV} = \frac{(\text{Total Assets} - \text{Total Liabilities})}{\text{No. of Units}}$$

### 2) Holding Period Return

$$\text{HPR} = \frac{(\text{NAV}_1 - \text{NAV}_0) + \text{CG} + \text{I}}{\text{NAV}_0}$$

Return in case the dividend and capital gains are reinvested

$$\text{HPR} = \frac{(N_1 - \text{NAV}_1) + (N_0 - \text{NAV}_0)}{(N_0 - \text{NAV}_0)}$$

### 3) Return earned by Mutual Funds

$$r_2 = \frac{1}{1 - \text{Initial exp.}} \times r_1 + \text{recurring exp.}$$

Where,

$r_2$  = Return desired by Investor

$r_1$  = Return earned by Mutual Funds

### 4) Expense Ratio

$$\text{ER} = \frac{\text{Expenses incurred per unit}}{\text{Average NAV}}$$

$$\text{ER} = \frac{\text{Expenses}}{\text{Average value of portfolio}}$$

## Chapter 8 Derivatives

### 1) Forwards [OTC Market]

| Basis      | Time Value of Money                  | Derivatives                          |
|------------|--------------------------------------|--------------------------------------|
| Annual     | $A=P(1+r)^t$                         | $F=S(1+r)^t$                         |
| Multiple   | $A=P\left(1+\frac{r}{n}\right)^{nt}$ | $F=S\left(1+\frac{r}{n}\right)^{nt}$ |
| Continuous | $A=Pe^{rn}$                          | $F=Se^{rn}$                          |

#### - Hedging with Futures

$$N = \frac{\text{Value to be hedged}}{\text{Futures Contract Value}} \times \text{Risk to be reduced}$$

$$\text{Contract Values} = \text{Futures Value} \times \text{Lot Size}$$

### 2) Binomial Model

$$\text{Option Value} = \frac{C_u \times p + C_d \times (1-p)}{(1+r)}$$

Where,

P is the probability of price moving upwards

r is the risk free rate of interest

t is the time interval

$C_u$  is the options value at upper level

$C_d$  is the options value at lower level

Also, P can be calculated using this formula

$$p = \frac{(1+r)-d}{u-d}$$

Where,

$$u = \frac{\text{stock price at upper level}}{\text{spot price}},$$

$$d = \frac{\text{stock price at lower level}}{\text{spot price}}$$

or,

u= volatility of price moving upwards,

d= volatility of price moving downwards.

**3) Risk Neutral Method**

$$\text{Spot Price} = \frac{\text{Stock Price at upper level} \times p + \text{Stock Price at lower level} \times (1-p)}{1+r}$$

$$\text{Spot Price} = \frac{S_u \times p + S_d \times (1-p)}{1+r}$$

Where,

$S_u$  is the Stock Price at upper level

$S_d$  is the Stock Price at lower level

**4) Black Scholes Model**

$$C_0 = S \times N(d_1) - Ke^{-rt} \times N(d_2)$$

Where,

$$d_1 = \frac{\ln\left(\frac{S}{K}\right) + \left(r + \frac{\sigma^2}{2}\right)t}{\sigma\sqrt{t}}, \quad d_2 = d_1 - \sigma\sqrt{t}$$

$S$ =current stock price

$K$ =strike price of the option

$t$ =time remaining until expiration

$r$ =current continuously compounded risk free interest rate

$\sigma$ =standard deviation of continuously compounded annual return

$\ln$ =natural logarithm

$N(x)$ =Standard normal cumulative distribution function

$e$ =exponential function

**Adjusting for Dividends**

$$\text{Call Option} = C_0 = Se^{-yt} \times N(d_1) - Ke^{-rt} \times N(d_2)$$

$$\text{Put Option} = P_0 = Ke^{-rt} \times [1 - N(d_2)] - Se^{-yt} \times [1 - N(d_1)]$$

Where,

$$d_1 = \frac{\ln\left(\frac{S}{K}\right) + \left(r - y + \frac{\sigma^2}{2}\right)t}{\sigma\sqrt{t}}, \quad d_2 = d_1 - \sigma\sqrt{t}$$

**5) Put Call Parity Theory**

$$S + P_0 = C_0 + \text{PV of Exercise price of the stock}$$

Where,

$S$  = Current price of the underlying asset

$P$  = Price (Premium) of the put option

$C_0$  = Price (Premium) of the call option

## 6) Portfolio Replicating Theory

$\Delta$  = Number of units of the underlying asset bought =  $(C_u - C_d) / (S_u - S_d)$

Where,

$\Delta$  = Delta/ Hedge Ratio

$C_u$  = Value of the call if the stock price is  $S_u$

$C_d$  = Value of the call if the stock price is  $S_d$

According to the Replicating Portfolio Model, value of the option can be calculated as follows

### Call Option

$C_0$  = Buy Delta Stock - Borrowing required to replicate the portfolio

Where,

$C_0$  = value of the call option

Borrowing needed to replicate the option = PV of  $[\Delta \times S_d - \text{Option value at } S_d]$

### Put Option

$P_0$  = Investment required - Sell Delta Stock

Where,

$P_0$  = value of the put option

Lending needed to replicate the option = PV of  $[\Delta \times S_u + \text{Option value at } S_u]$

## 7) Option Greeks

| Options Greeks |          |   |   |
|----------------|----------|---|---|
| Greeks         | Symbol   | Represents  | Formula,  |
| Delta          | $\delta$ | Delta represents the change in the Option value with ₹1 change in the Stock Price             | $\text{Delta } (\delta) = \frac{\Delta V_o}{\Delta S_o}$    |
| Gamma          | $\gamma$ | Gamma represents the change in the Options Delta with ₹1 change in the Stock Price            | $\text{Gamma } (\gamma) = \frac{\Delta \delta}{\Delta S_o}$ |
| Rho            | $\rho$   | Rho represents the change in the Options Value with 1% change in the Interest Rates           | $\text{Rho } (\rho) = \frac{\Delta V_o}{\Delta r}$          |
| Theta          | $\theta$ | Theta represents the change in the Options Value with 1 day change in the time to expiry      | $\text{Theta } (\theta) = \frac{\Delta V_o}{\Delta t}$      |
| Vega           | $\nu$    | Vega represents the change in the Options Value with 1% change in the volatility of the stock | $\text{Vega } (\nu) = \frac{\Delta V_o}{\Delta \sigma}$     |

Where,  $V_o$ = value of the option,  $S_o$ = Spot price of the stock,  $r$ = rate of Interest,  $t$ = time to expiration

## 8) Intrinsic Value [IV] & Time Value [TV]

### 1. Intrinsic Value

For a call option,  $IV = \text{Max}(0, S-K)$

For a put option,  $IV = \text{Max}(0, K-S)$

### 2. Time Value

Time value = Option Premium – Intrinsic Value

## 9) Option Payoff

| Position                     | Option | Payoff                       | Effect                         |
|------------------------------|--------|------------------------------|--------------------------------|
| Long (Holder of the option)  | Call   | Payoff= $\text{Max}(0, S-K)$ | Limited Loss, Unlimited Profit |
|                              | Put    | Payoff= $\text{Max}(0, K-S)$ | Limited Profit, Limited Loss   |
| Short (Writer of the option) | Call   | Payoff= $\text{Min}(0, K-S)$ | Limited Profit, Unlimited Loss |
|                              | Put    | Payoff= $\text{Min}(0, S-K)$ | Limited Loss, Limited Profit   |

Break Even = Break-even price is the price at which your net payoff is “0”

|       | Call      | Put       |
|-------|-----------|-----------|
| Long  | $S-K-P=0$ | $K-S-P=0$ |
| Short | $K-S+P=0$ | $S-K+P=0$ |

## 10) Write a short note on Factors affecting Option Valuation

| Factors Affecting Option Valuation (Option Premium) |          |      |  |     |   |
|---|----------|------|--|-----|---|
| Factor  |          | Call | Explanation  | Put | Explanation   |
| <b>Stock Price</b>                                  | Increase | ▲    | For a given strike price(55) increase in the stock price(60,70,80) increases the demand for call hence higher premium and vice-versa                                 | ▼   | For a given strike price(55) increase in the stock price(30,40,50) decreases the demand for put hence lower premium and vice-versa                                    |
|   | Decrease | ▼    |  | ▲   |   |
| <b>Exercise Price</b>                               | Increase | ▼    | For a given stock price (55) increase in the strike price (30,40,50) decreases the demand for call hence lower premium and vice-versa                                | ▲   | For a given stock price (55) increase in the strike price (60,70,80) increases the demand for put hence higher premium and vice-versa                                 |
|   | Decrease | ▲    |  | ▼   |   |
| <b>Time to Expiration</b>                           | More     | ▲    | More the time to expiry, more are the chances for Option to be In The Money, hence higher premium & vice-versa   | ▲   | More the time to expiry, more are the chances for Option to be In The Money, hence higher premium & vice-versa  |
|   | Less     | ▼    |  | ▼   |   |
| <b>Volatility</b>                                   | More     | ▲    | More the volatility, more are the chances for Option to be In The Money, hence higher premium & vice-versa   | ▲   | More the volatility, more are the chances for Option to be In The Money, hence higher premium & vice-versa  |
|   | Less     | ▼    |  | ▼   |   |
| <b>Interest Rate</b>                                | Increase | ▲    | Increase in interest rate increases the interest income that can be earned on money saved in buying call option, which increases demand for call and premium thereon | ▼   | Increase in interest rate increases the opportunity cost of interest income on put option which decreases demand for put and premium thereon (however less practical) |
|   | Decrease | ▼    |  | ▲   |   |

1) **Premium/Discount**

| Premium/(Discount) in Base Currency   | Premium/(Discount) in Counter Currency   |
|---|--|
| $\frac{F-S}{S} \text{ or } \frac{F}{S}-1$   | $\frac{S-F}{F} \text{ or } \frac{S}{F}-1$  |
| <p>Where,<br/>                     F = Forward exchange rate<br/>                     S = Spot exchange rate<br/>                     N= Number of months of the forward contract</p> | <p>Where,<br/>                     F = Forward exchange rate,<br/>                     S = Spot exchange rate<br/>                     N= Number of months of the forward contract</p> |

2) **Interest Rate Parity Theory**

When Exchange Rates are in **Direct Quote**

$$\frac{1+r_d}{1+r_f} = \frac{F}{S}$$

When Exchange Rates are in **Indirect Quote**

$$\frac{1+r_f}{1+r_d} = \frac{F}{S}$$

Where,

$r_d$  = Rate of interest in domestic market

$r_f$  = Rate of interest in foreign market

F = Forward rate of the foreign currency

S = Spot rate of the foreign currency

3) **Purchasing Power Parity Theory**

$$F = S \times \frac{1+i_d}{1+i_f}$$

Where,

$i_d$  = Inflation rate in domestic market

$i_f$  = Inflation rate in foreign market

F = Forward rate for foreign currency

S = Spot rate for foreign currency

4) **International Fisher Effect**

$$\Delta S \approx R_d - R_f$$

Or

$$F = S \times \frac{1 + R_d}{1 + R_f}$$

Where,

$R_d$  = Nominal Interest rate of domestic country

$R_f$  = Nominal Interest rate of foreign country

### 5) Broken Period Forward Rate

| Broken Period Forward Rate  |                                  |               |                              |
|---|----------------------------------|---------------|------------------------------|
| For broken period the convenient way is to interpolate the rates between the two standard day |                                  |               |                              |
| Spot ₹/\$<br>47.0725/745  | 1m ₹/\$<br>133/140               | 3m<br>145/160 | 6m<br>155/175                |
| <b>Bid Rate</b>   | $145 + (155 - 145) \times 25/90$ | 148           | $47.0725 + 0.0148 = 47.0873$ |
| <b>Ask Rate</b>   | $160 + (175 - 160) \times 25/90$ | 164           | $47.0745 + 0.0164 = 47.0909$ |
| Spot ₹/\$<br>47.0725/745  | 1m ₹/\$<br>140/133               | 3m<br>160/145 | 6m<br>175/155                |
| <b>Bid Rate</b>   | $160 + (175 - 160) \times 25/90$ | 164           | $47.0725 - 0.0164 = 47.0561$ |
| <b>Ask Rate</b>   | $145 + (155 - 145) \times 25/90$ | 148           | $47.0745 - 0.0148 = 47.0597$ |

### 6) Nostro, Vostro and Loro Account

| Nostro, Vostro & Loro Account |                                |  |  |
|-------------------------------|--------------------------------|--|--|
| <b>Nostro Account</b>         | “Our account with your bank”   | Nostro accounts are generally held in a foreign country (with a foreign bank), by a domestic bank (from our perspective, our bank). It obviates that account is maintained in that foreign currency. | State Bank of India account in Bank of America is a Nostro Account for State Bank of India |
| <b>Vostro Account</b>         | “Your account with our bank”   | Vostro accounts are generally held by a foreign bank in our country (with a domestic bank). It generally maintained in Indian Rupee (if we consider India)   | State Bank of India account in Bank of America is a Vostro Account for Bank of America     |
| <b>Loro Account</b>           | “Your account with their bank” | Loro accounts are generally held by a 3rd party bank, other than the account maintaining bank or with whom account is maintained.  | State bank of India account in Bank of America is Loro Account for ICICI Bank              |

### 1) Forward Rate Agreement

$$\text{Settlement} = \frac{(N)(RR-FR)\left(\frac{dtm}{DY}\right)}{\left[1+RR\left(\frac{dtm}{dy}\right)\right]} \times 100$$

Where,

N = the notional principal amount of the agreement;

RR = Reference Rate for the maturity specified by the contract prevailing on the contract settlement date; typically LIBOR or MIBOR

FR = Agreed-upon Forward Rate; and

dtm = maturity of the forward rate, specified in days (FRA Days)

DY = Day count basis applicable to money market transactions which could be 360 or 365 days.

If LIBOR > FR the seller owes the payment to the buyer, and if LIBOR < FR the buyer owes the seller the absolute value of the payment amount determined by the above formula.

### 2) Value of the Swap

$$V_{\text{swap}} = B_{\text{fl}} - B_{\text{fix}}$$

### 3) Adjusted Net Present Value

$$\text{APV} = \text{NPV} + \text{PV of Tax Shield on Interest} + \text{PV of Interest Subsidies}$$

### Methods of Valuation

#### 1) Asset Based

Book Value = Total Assets – Long Term Debt

- Total Assets = Fixed Assets + Intangible Assets + Current Assets – Current Liabilities
- This can also be equated to share capital plus free reserves

#### 2) Earnings Based

$$\text{Value of the Equity} = \frac{\text{EAT}}{K_e}$$

$$\text{Value of the Company} = \frac{\text{EBITDA}}{K_o}$$

#### 3) Enterprise Value Based

Enterprise Value = Market Value of Equity

+Market Value of Preference

+Market Value of Debt

+Minority Interest

- Cash & Cash Equivalent

#### 4) Other Methods

##### 1. Economic Value Added

$$\text{EVA} = \text{NOPAT} - (\text{Invested Capital} * \text{WACC})$$

Or

$$\text{EVA} = \text{NOPAT} - \text{Capital Charge}$$

##### 2. Market Value Added

$$\text{MVA} = \text{Market Value} - \text{Book Value}$$

##### 3. Shareholders Value Analysis

Steps involved in SVA computation:

1. Arrive at the Future Cash Flows (FCFs) by using mix of the 'value drivers'
2. Discount these FCF using WACC
3. Add the terminal value to the present values computed in step (b)

## 12. Corporate Valuation

4. Add market value of non-core assets
5. Reduce the value of debt from the result in step (d) to arrive at value of equity